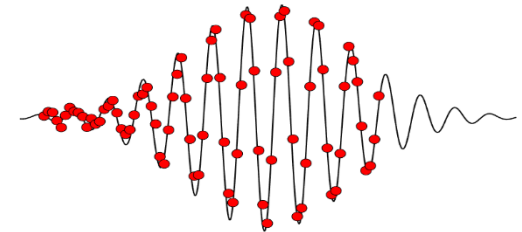


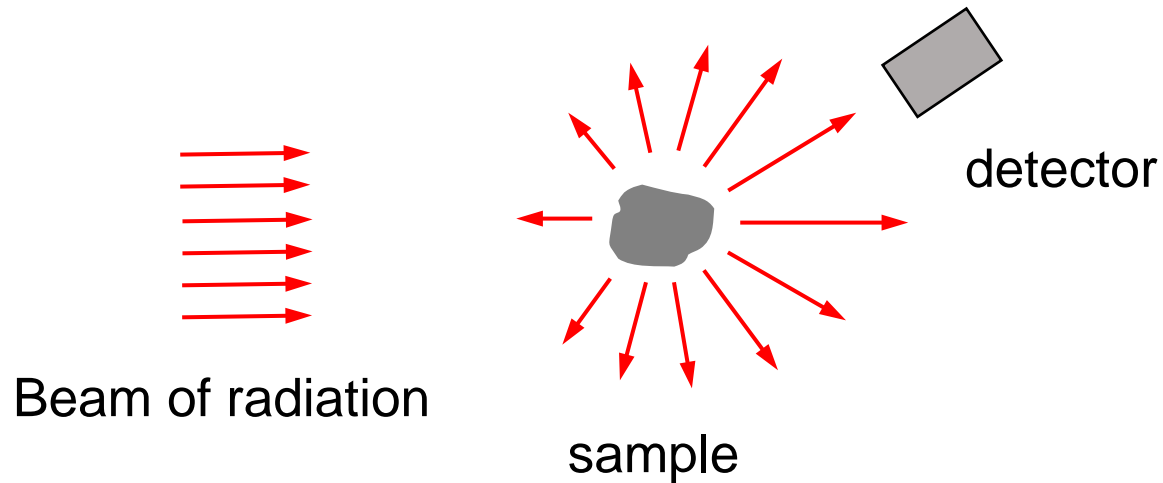
The neutron: properties and interactions

Andrew Boothroyd
Oxford University

- What is a neutron?
- How does it interact with matter?
- Prepare the ground for understanding the principles of neutron scattering



Scattering 'nuts and bolts'



- Source of radiation: photons, **neutrons**, electrons, atoms, ...
- Measure **distribution** of radiation scattered from a sample
- Form of **interaction** determines what you can measure
- Radiation must be **coherent** to measure correlations

Discovery of the neutron

1932 (Chadwick)

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Letters to the Editor

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Possible Existence of a Neutron

It has been shown by Bothe and others that beryllium when bombarded by α -particles of polonium emits a radiation of great penetrating power, which has an absorption coefficient in lead of about 0.3 (cm.)^{-1} . Recently Mme. Curie-Joliot and M. Joliot found, when measuring the ionisation produced by this beryllium radiation in a vessel with a thin window, that the ionisation increased when matter containing hydrogen was placed in front of the window. The

This again receives a simple explanation on the neutron hypothesis.

If it be supposed that the radiation consists of quanta, then the capture of the α -particle by the Be^9 nucleus will form a C^{13} nucleus. The mass defect of C^{13} is known with sufficient accuracy to show that the energy of the quantum emitted in this process cannot be greater than about 14×10^6 volts. It is difficult to make such a quantum responsible for the effects observed.

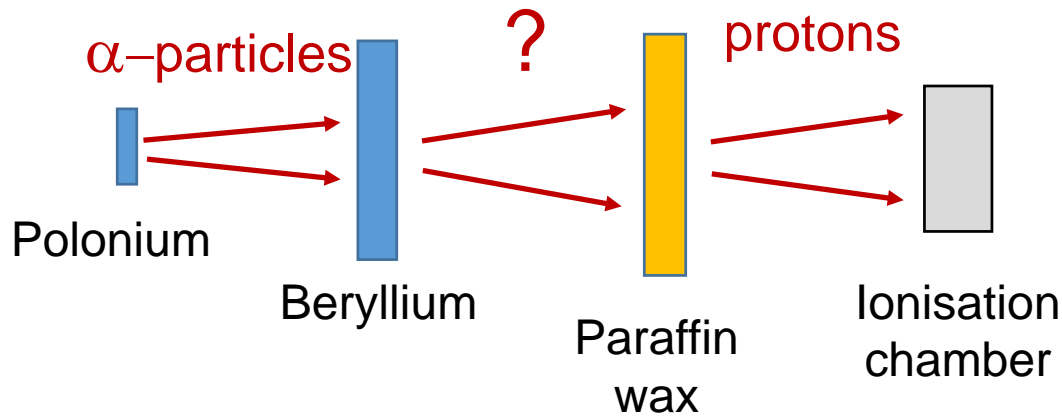
It is to be expected that many of the effects of a neutron in passing through matter should resemble those of a quantum of high energy, and it is not easy to reach the final decision between the two hypotheses. Up to the present, all the evidence is in favour of the neutron, while the quantum hypothesis can only be upheld if the conservation of energy and momentum be relinquished at some point.

J. CHADWICK.

Cavendish Laboratory,

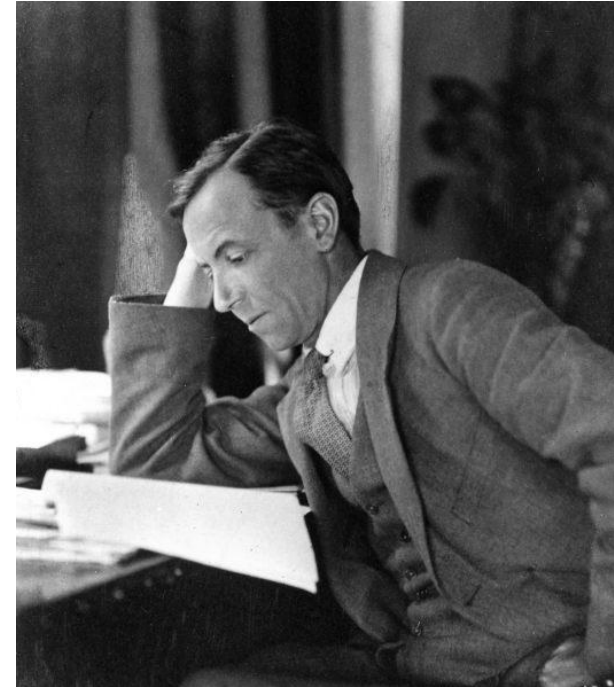
Discovery of the neutron

I. Curie and F. Joliot, 1932



Chadwick, 1932

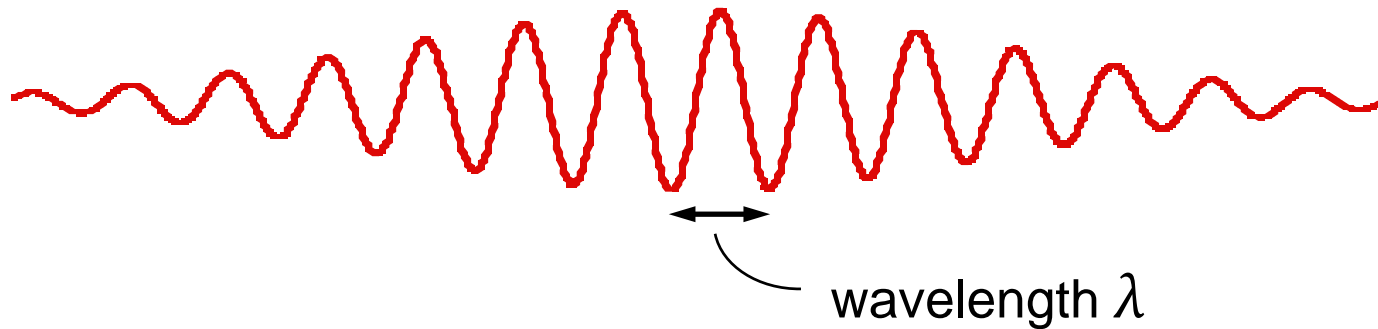
? = neutrons



James Chadwick (1891-1974)
Nobel Prize in Physics (1935)

Neutrons are particles and waves!

- matter wave:



- Kinematics (de Broglie):

momentum: $p = h/\lambda$ ($h = \text{Planck's constant}$)

$$\mathbf{p} = \hbar \mathbf{k} \quad (\mathbf{k} = \text{wavevector, } k = 2\pi/\lambda)$$
$$(\hbar = h/2\pi)$$

kinetic energy: $E = \frac{1}{2}m_n v^2 = p^2/2m_n$

$$\rightarrow E = h^2/(2m_n \lambda^2) = \hbar^2 k^2/2m_n$$

Scattering kinematics

- momentum transfer

$$\hbar\mathbf{Q} = \hbar\mathbf{k}_i - \hbar\mathbf{k}_f$$

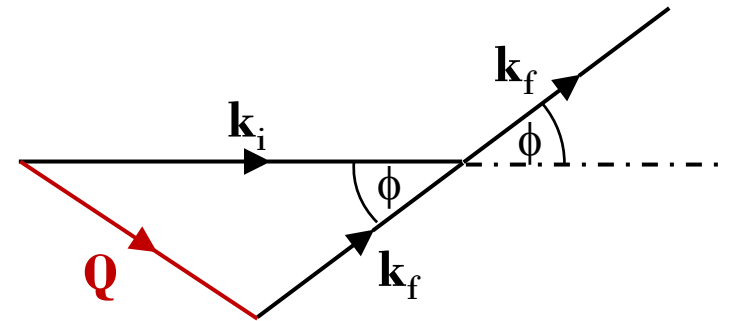
- energy transfer

$$\begin{aligned}\hbar\omega &= E_i - E_f \\ &= \hbar^2(k_i^2 - k_f^2)/2m_n\end{aligned}$$

- a scattering event is characterised by (\mathbf{Q}, ω)

Elastic scattering (diffraction): $\hbar\omega = 0$

Inelastic scattering (spectroscopy): $\hbar\omega \neq 0$



scattering triangle

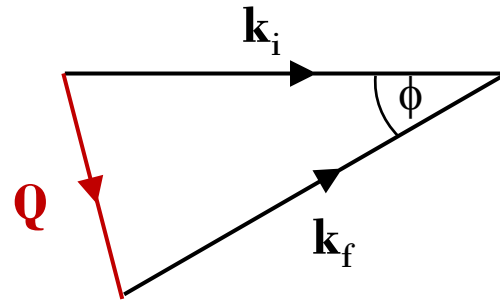
Elastic scattering (diffraction): $\hbar\omega = 0$

- Scattering vector

$$\mathbf{Q} = \mathbf{k}_i - \mathbf{k}_f$$

BUT sometimes written

$$\mathbf{Q} = \mathbf{k}_f - \mathbf{k}_i$$



isosceles scattering triangle

Beware of crystallographers!

Particle properties of the neutron

- Mass = 1.675×10^{-27} kg (= $1.001 m_p$)
- Charge = 0
- Mean lifetime \approx 15 min
- Spin = $\frac{1}{2}$
- Magnetic moment = $1.91 \mu_N$ ($\sim 0.001 \mu_B$)

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de Broglie: $p = h/\lambda$ ($h = \text{Planck's constant}$)

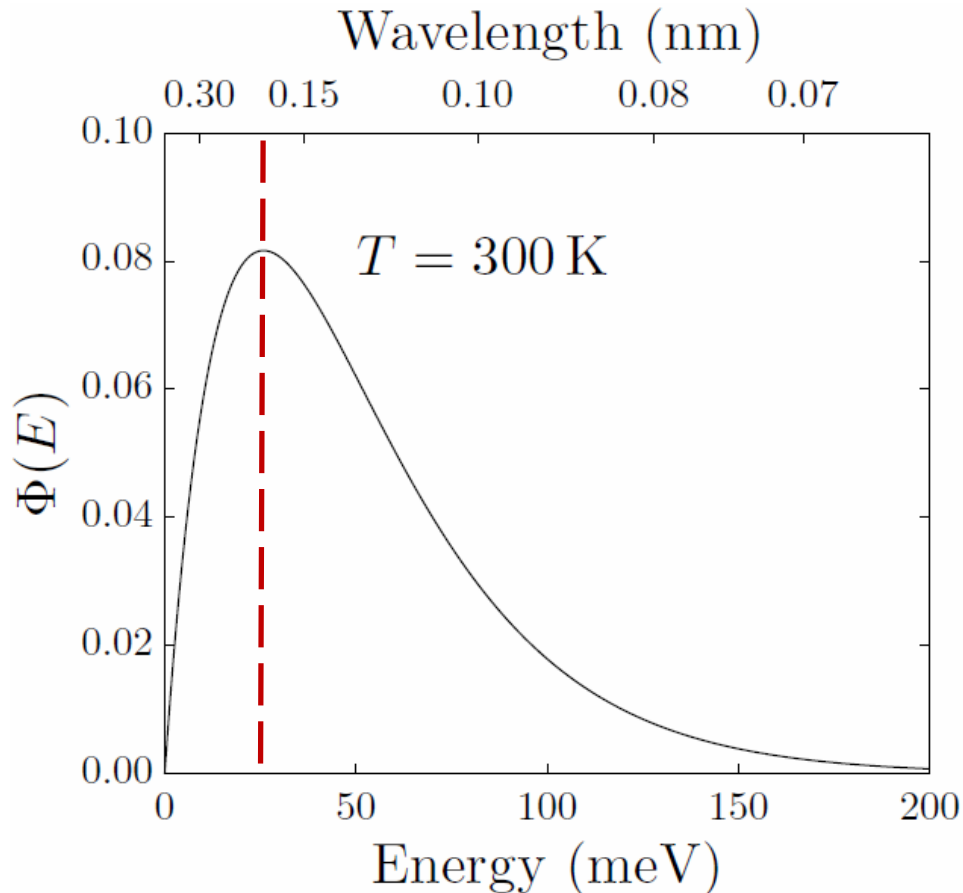
$$\rightarrow E = h^2/(2m_n \lambda^2)$$

hence $E = 25 \text{ meV} \rightarrow v = 2,200 \text{ ms}^{-1}$ and $\lambda = 0.18 \text{ nm}$

$E \sim$ energy of thermal excitations in condensed matter

$\lambda \sim$ inter-atomic distances in condensed matter

Thermal neutrons



neutrons are well matched to probe the atomic-scale structure and dynamics of substances at normal operating temperatures

Comparison with x-rays

X-rays are electromagnetic radiation (photons)

$$\begin{aligned}\text{Einstein: } E &= hf && (f = \text{frequency}) \\ &= hc/\lambda && (c = f\lambda = \text{speed of light} \\ & && = 3.0 \times 10^8 \text{ ms}^{-1})\end{aligned}$$

$$\text{hence } E = 6.9 \text{ keV} \longrightarrow \lambda = 0.18 \text{ nm (x-rays)}$$

$$E = 25 \text{ meV} \longrightarrow \lambda = 0.18 \text{ nm (neutrons)}$$

Neutrons better suited to low energy dynamics

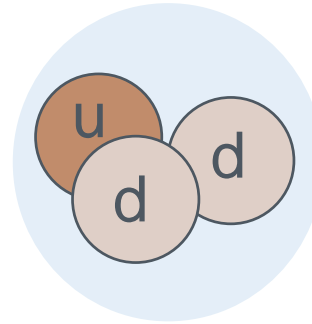
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Particle properties of the neutron

Standard model:
neutron composed of 3 quarks

Charge = 0



u: $+\frac{2}{3}e$
d: $-\frac{1}{3}e$

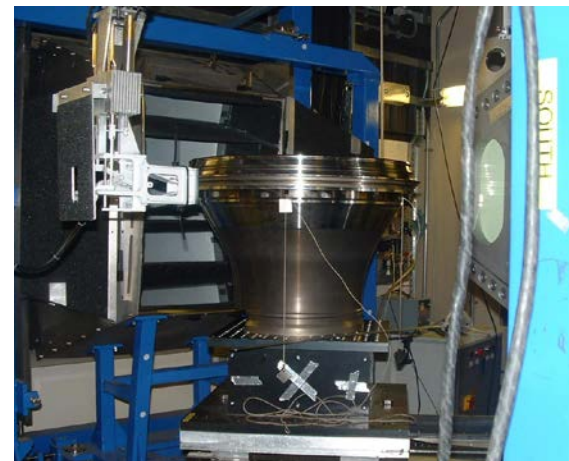
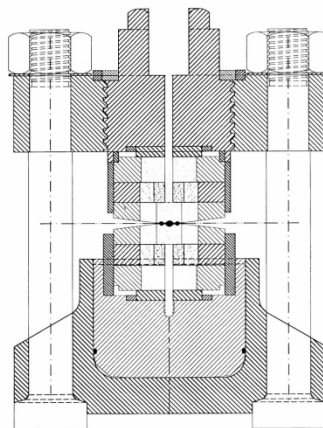
Electric dipole moment: $d < 4.6 \times 10^{-47} \text{ C m}$
(water molecule: $d = 6.1 \times 10^{-30} \text{ C m}$)

Neutrons do not feel electrostatic forces

→ *neutrons are highly penetrating*

Neutron penetration depth ~ 1 cm

- **bulk probe**
- **surface effects can usually be neglected**
(exception is neutron reflectometry)
- **non-destructive**
- **can study samples in complex sample environments,**
e.g. cryostats, magnets, pressure cells, ...



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Neutrons last long enough to perform experiments

Particle properties of the neutron

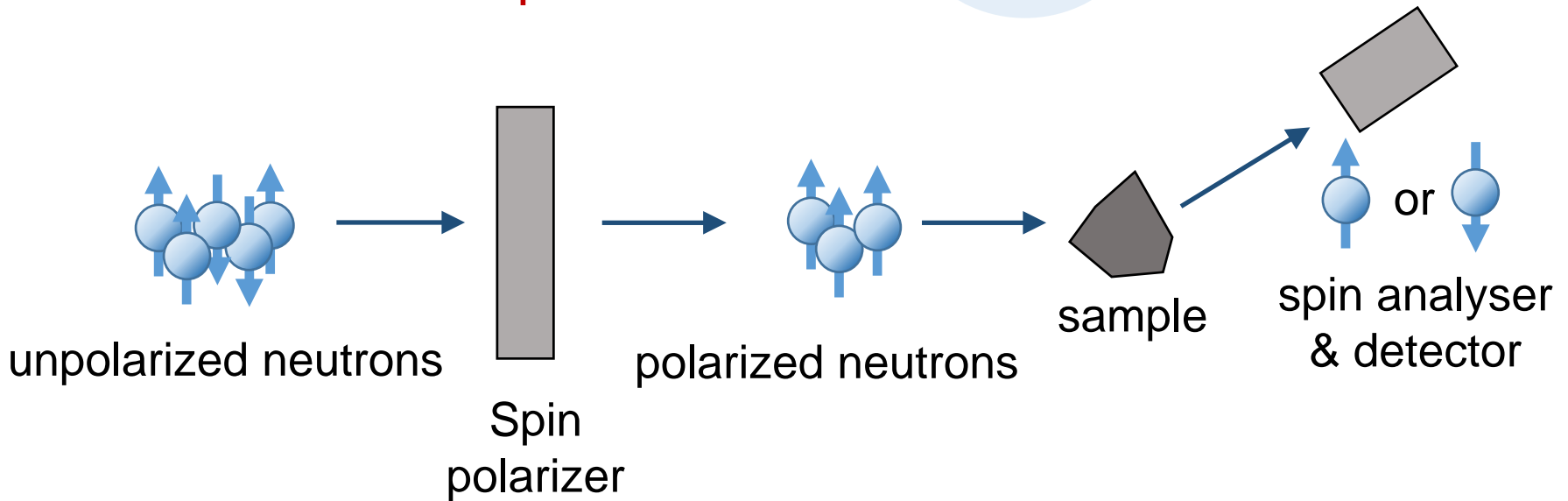
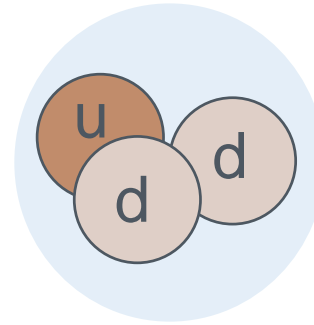
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Neutrons can be spin-polarized

Polarized neutrons

Quarks are spin-1/2 particles

→ neutron has spin = 1/2



measure polarization-dependent scattering intensities

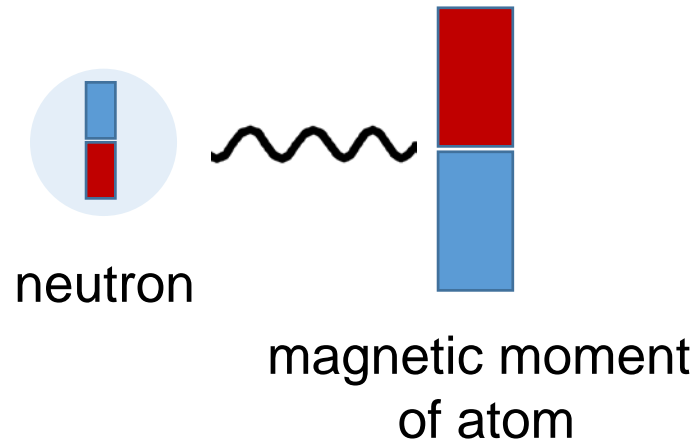
→ neutron polarization analysis

Particle properties of the neutron

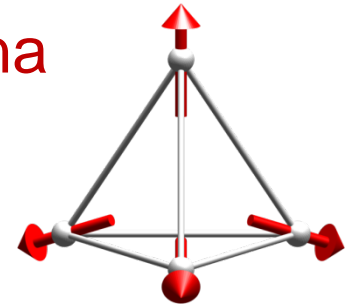
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- Charge = 0
- Mean lifetime \approx 15 min
- Spin = $\frac{1}{2}$
- Magnetic moment = $1.91 \mu_N$ ($\sim 0.001 \mu_B$)

→ Magnetic neutron scattering

Magnetic scattering



Can study a wide range of magnetic phenomena
e.g. magnetic structures



Neutron interactions with matter

Neutrons interact with

1. Atomic nuclei (strong nuclear force — short-range)
2. Magnetic fields from unpaired electrons

In both cases, the interaction is **very weak**

Strengths:

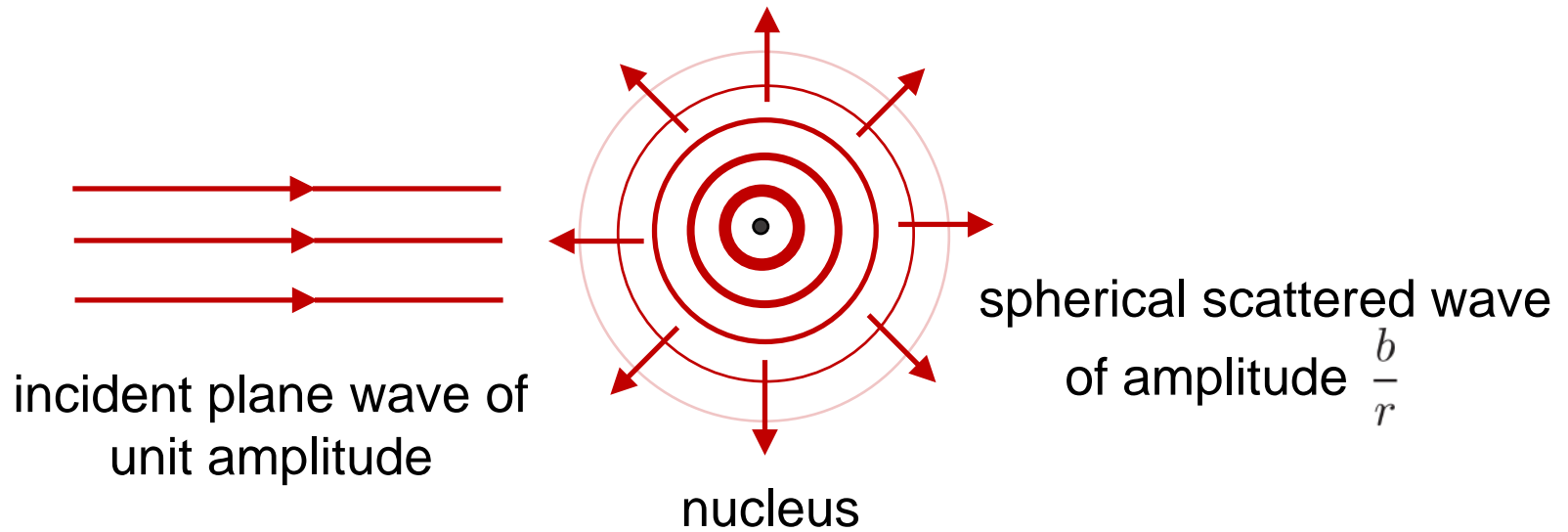
1. Neutrons probe the bulk (~1 cm)
2. Neutrons are non-destructive
3. Intensity can be calibrated
4. Theory is quantitative

Weaknesses:

Sample size is important:

- single crystals: ~1 mm³ (diffraction)
~1 cm³ (spectroscopy)
- powders/fluids: ~1 g (diffraction)
~10 g (spectroscopy)

Scattering from bound nuclei



Nuclear scattering length

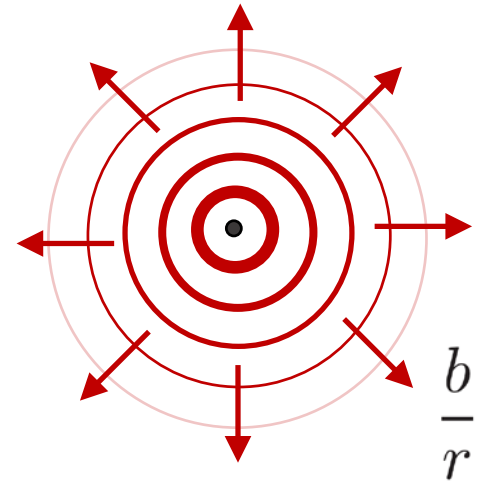
Nucleus is very small $\sim 10^{-15}$ m

Formal theory uses a **pseudopotential**:

$$V_N(\mathbf{r}) = \frac{2\pi\hbar^2}{m_n} b \delta(\mathbf{r})$$

b = nuclear scattering length

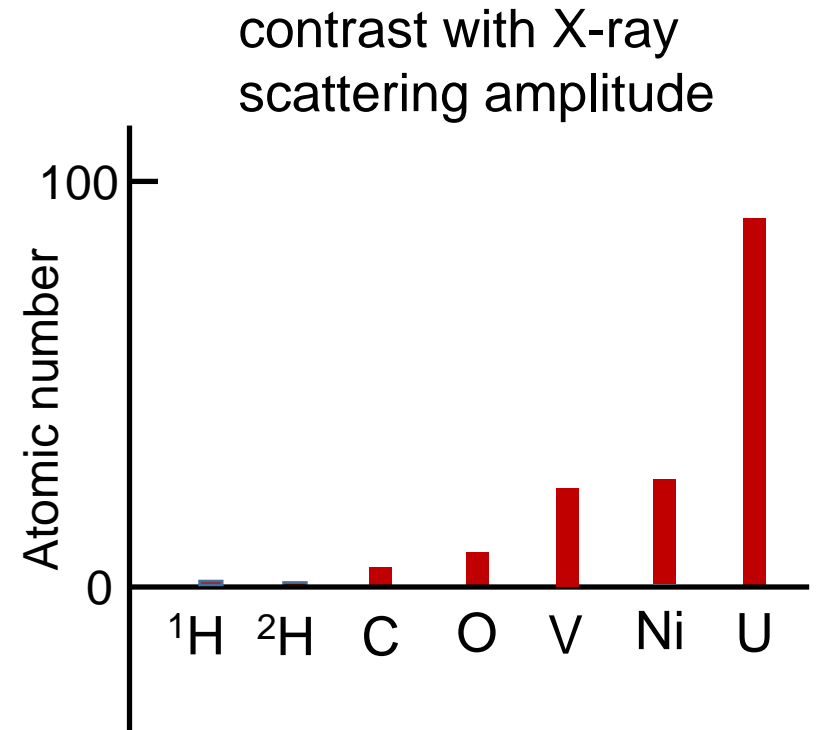
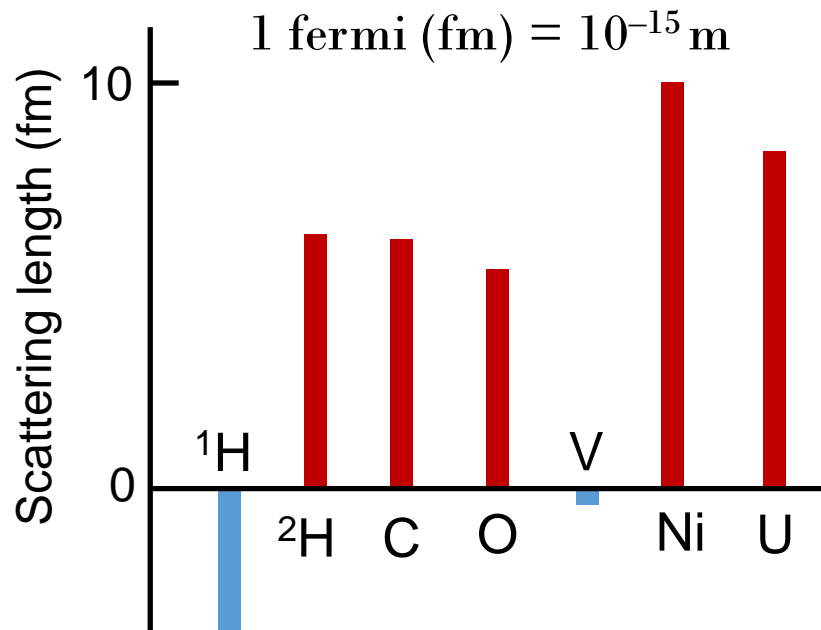
b measures **both** the **amplitude** of scattered wave
and the **strength** of the nuclear potential

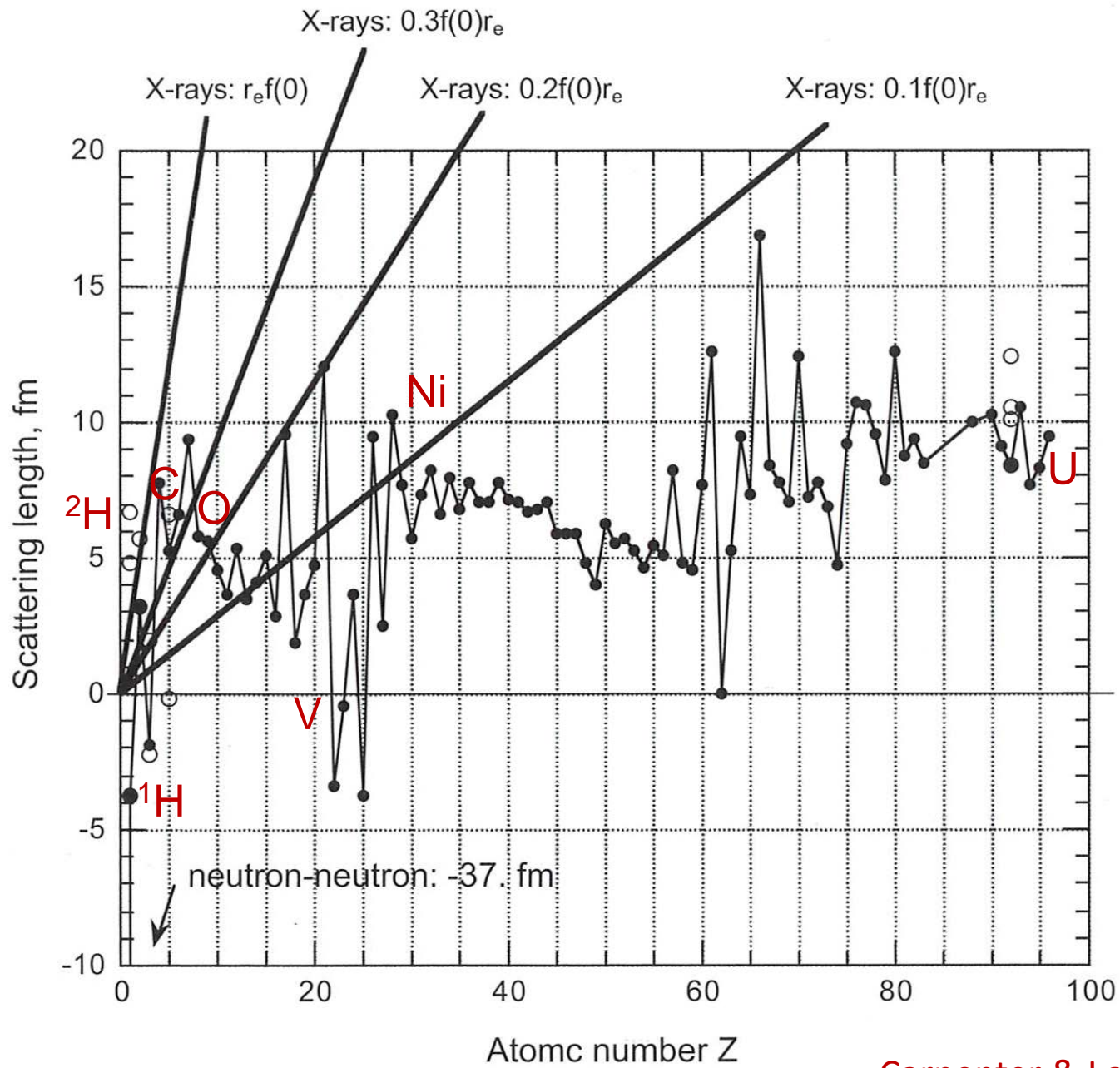


Nuclear scattering length

b varies irregularly with atomic number

b also depends on isotope and on nuclear spin orientation



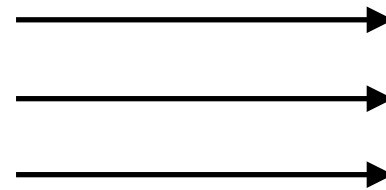


Cross-sections

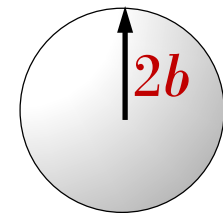
scattering amplitude $\sim b$ [length]

scattering intensity $\sim b^2$ [area]

$2b$ = effective radius of nucleus



neutron beam



nucleus

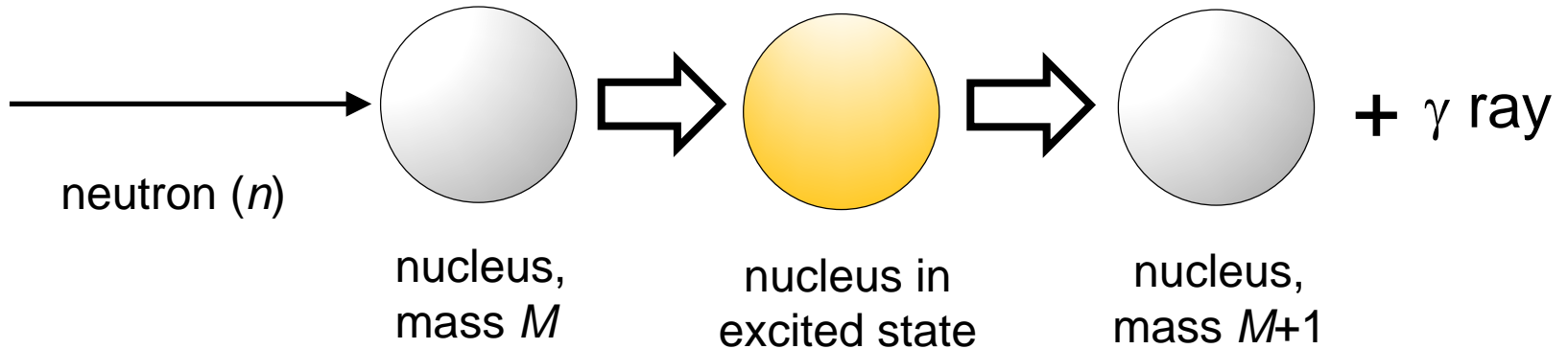
$\sigma_s = 4\pi b^2$ = effective cross-sectional area of nucleus

Scattering probabilities are expressed as cross-sections

unit: 1 barn (b) = 10^{-28} m^2

Absorption cross-sections

(n,γ) reaction:

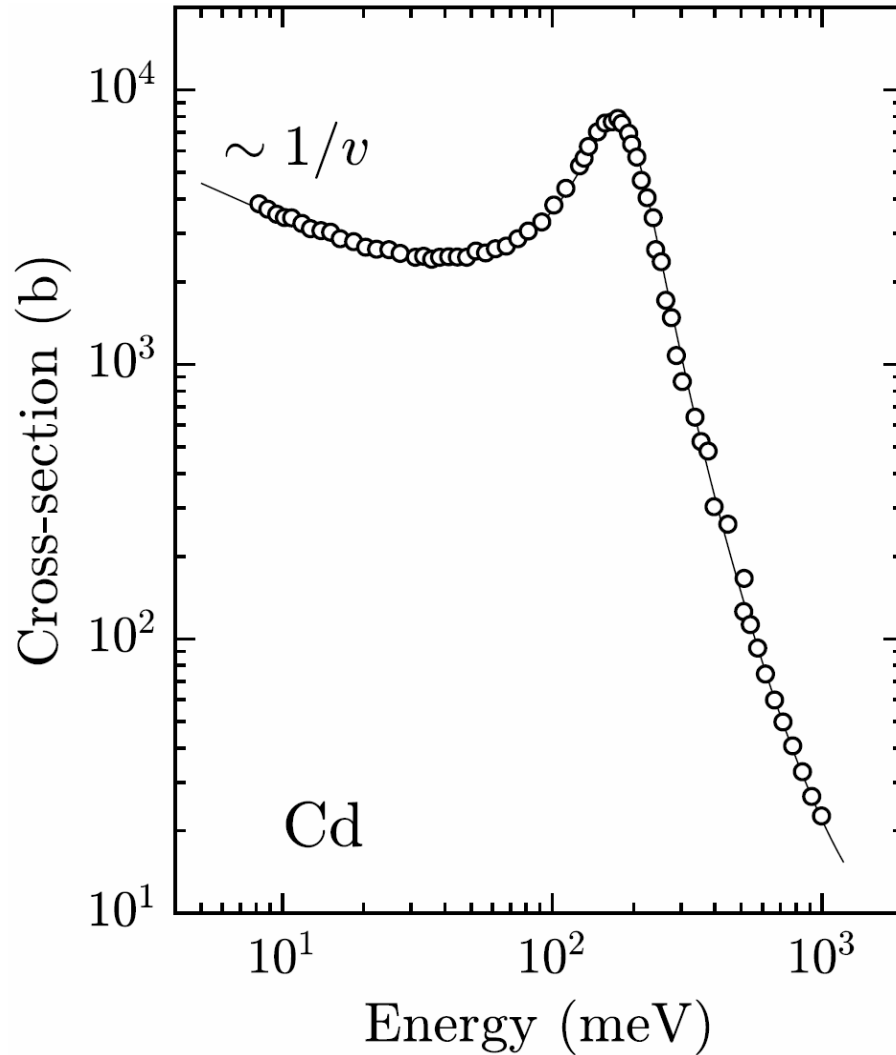


Strongly absorbing nuclei:

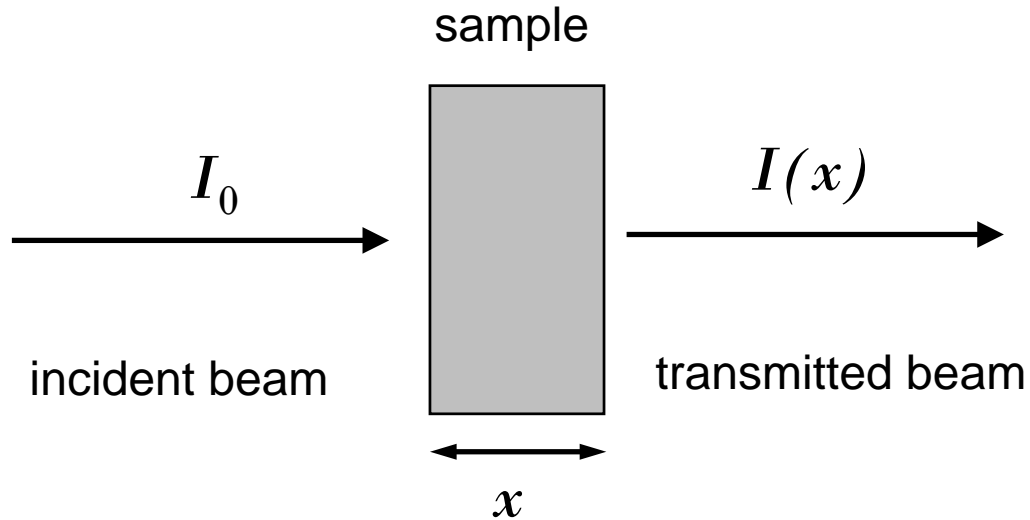
^3He , ^{10}B , ^{113}Cd , ^{149}Sm , ^{151}Eu , ^{155}Gd , ^{157}Gd

Reaction probability is described by the **absorption cross-section** σ_a , which is dependent on neutron energy

Absorption cross-section of cadmium



neutron transmission



- Beer-Lambert law:

$$I(x) = I_0 \underbrace{\exp(-n\sigma x)}_{\text{transmission}}$$

n = number density

$$\sigma = \sigma_a + \sigma_s$$

Comparison with x-rays

neutrons

- good for low energies
- bulk probe: mm to cm
- large samples required
- non-destructive
- good for light elements
- scattering is isotope-dependent
- can obtain cross-sections quantitatively
- theory is accurate and understood

X-rays

- good for high energies
- probes nm to μm
- can measure small samples
- X-rays can affect sample
- good for heavy elements
- scattering depends on atomic number
- difficult to be quantitative
- theory still being developed

Strength of neutrons

*It might well be said that, if the neutron
did not exist, it would need to be invented!*

(B. N. Brockhouse, 1983)